Engineering Note 17.1

## Measuring Thiele-Small parameters of a loudspeaker

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## 1. DC resistance $R_{D C}$.

Measure, using an ohmmeter or bridge.

## 2. Total $Q$-factor, $Q_{t}$

Requires: Audio oscillator and amplifier, frequency counter, audio voltmeter, $1 \mathrm{k} \Omega 10$ W resistor, calculator!

Connect the oscillator, to the amplifier, thence to the resistor and loudspeaker in series. Set the amplifier output voltage to 10 V (thus passing 10 mA through the loudspeaker.)
Adjust the oscillator frequency for maximum voltage across the loudspeaker and check for zero phase condition with Lissajou's Figure. Call this frequency $f_{0}$.
Note the voltage across the loudspeaker. Divide by 10 mA to get the resistance $R_{0}$. Divide $R_{0}$ by $R_{D C}$, call the result $r_{0}$. Calculate the square root of $r_{0}$.
Adjust the oscillator frequency so that the loudspeaker voltage corresponds to a resistance (DC resistance) $\times \sqrt{ } r_{0}$. Note the two frequencies $f_{1}$ and $f_{2}$. Check that $\sqrt{ }\left(f_{1}\right.$ $\times f_{2}$ ) is nearly equal to $f_{0}$.

Calculate $Q_{T}=\left\{\sqrt{ }\left(f_{1} \times f_{2}\right)\right\} /\left\{\vee r_{0} \times\left(f_{2}-f_{1}\right)\right\}$

## 3. Equivalent volume $V_{\text {as }}$

The 'official' method ( IEC/EN 60268-5) requires a vented box of suitable dimensions with bung for vent.

Alternative method using added mass (not very accurate!)
Determine the new resonance frequency $f_{3}$ with a known mass $M$ added to the cone (Blu-Tac, or a wire ring fitted round the voice-coil former: NOT making a shorted turn!).
( $M$ should be approximately equal to the cone mass, so that the resonance frequency is reduced to about 0.7 of its normal value.)
Calculate $C_{m s}=\left(f_{0}{ }^{2}-f_{3}{ }^{2}\right) / M f_{1}{ }^{4}$ and then $C_{a s}=C_{m s} S_{d}{ }^{2}$, where $S_{d}$ is the effective diaphragm area.
Then $V_{a s}=\rho_{0} C^{2} C_{a s}=139636.48 \times C_{a s}$. BUT 139636.48 is SILLY! Use 140000 !

## Example: Hokutone 5 inch 120F30, 8 ohms

## Determining $Q_{T}$

DC resistance 7.73 ohms Resonance at 175 Hz , with voltage 0.186 V from 10 mA current, i.e. resistance 18.6 ohms. $r_{0}=2.406, \sqrt{ } r_{0}=1.551,7.73 \times 1.551=12$. Voltage corresponding to 12 ohms is 0.12 V . Frequencies where voltage is 0.12 V are 156 Hz and 198 Hz . Check: $\sqrt{ }(156 \times 198)=175.75-\mathrm{OK}$.
$Q_{T}=175.75 /\{1.551 \times(198-156)\}=2.7$
For reflex box use, the $Q_{T}$ should ideally be down in the 0.3 range.

## Determining $V_{\text {as }}$

Added mass 5 grams $=0.005 \mathrm{~kg}$. New resonance frequency $f_{3}=90 \mathrm{~Hz}$ (So 5 g is really too much: the resonance should have not gone below $0.7 \times 175=123 \mathrm{~Hz}$.)
Calculate $C_{m s}=\left(175^{2}-90^{2}\right) /\left(0.005 \times 175^{4}\right)=3.8 \times 10^{-5}$

Effective radius of cone $=50 \mathrm{~mm}$, so $\mathrm{S}_{d}{ }^{2}=6.17 \times 10^{-5}$
$C_{a s}=3.8 \times 10^{-5} \times 6.17 \times 10^{-5}=2.34 \times 10^{-9}$
Then $V_{a s}=2.34 \times 10^{-9} \times 140000=3.27 \times 10^{-4} \mathrm{~m}^{3}=0.33 \mathrm{~L}$
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## Data collection form

DC resistance $R_{D C}$ :
Free air resonance frequency $f_{0}$ :
Resonance voltage $V_{0}$ :
Resonance current $I_{0}$ :
Resonance resistance $R_{0}$ :
Resistance ratio $r_{0}$ :
Root of $r_{0}$ :
Off-resonance impedance:
Corresponding voltage or current:
Lower off-resonance frequency $f_{1}$ :
Upper off-resonance frequency $f_{2}$ :
Check: $f_{1} f_{2}=\quad f_{0}{ }^{2}=$
Calculate: $Q_{T}=\left\{\sqrt{ }\left(f_{1} \times f_{2}\right)\right\} /\left\{\sqrt{ } r_{0} \times\left(f_{2}-f_{1}\right)\right\}:$
Added mass $M$ :
New resonance frequency $f_{3}$ :
Calculate $C_{m s}=\left(f_{0}{ }^{2}-f_{3}{ }^{2}\right) / M f_{1}{ }^{4}$ :
Cone diameter $d_{D}$ :
Cone area $S_{D}$ :
Calculate $C_{a s}=C_{m s} S_{d}{ }^{2}$ :
Calculate $V_{a s}=140000 C_{a s}$ :

